JEE-Main Exam April, 2019 / 9-4-19 / Morning session

Physics

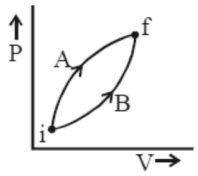
1. In the density measurement of a cube, the mass and edge length are measured as (10.00 ± 0.10) kg and (0.10 ± 0.01) m, respectively. The error in the measurement of density is :

   (a) 0.10 kg/m^3 (b) 0.31 kg/m^3 (c) 0.07 kg/m^3 (d) 0.01 kg/m^3

2. An HCl molecule has rotational, translational and vibrational motions. If the rms velocity of HCl molecules in its gaseous phase is $\bar{v}$, m is its mass and k_B is Boltzmann constant, then its temperature will be :

   (a) $\frac{m\bar{v}^2}{6k_B}$ (b) $\frac{m\bar{v}^2}{5k_B}$ (c) $\frac{m\bar{v}^2}{3k_B}$ (d) $\frac{m\bar{v}^2}{7k_B}$

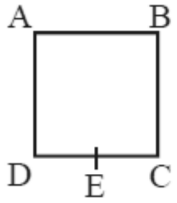
3. Following figure shows two processes A and B for a gas. If ΔQ_A and ΔQ_B are the amount of heat absorbed by the system in two cases, and ΔU_A and ΔU_B are changes in internal energies, respectively, then :



   (a) $\Delta Q_A = \Delta Q_B; \Delta U_A = \Delta U_B$ (b) $\Delta Q_A > \Delta Q_B; \Delta U_A = \Delta U_B$

   (c) $\Delta Q_A > \Delta Q_B; \Delta U_A > \Delta U_B$ (d) $\Delta Q_A < \Delta Q_B; \Delta U_A < \Delta U_B$

4. A wire of resistance R is bent to form a square ABCD as shown in the figure. The effective resistance between E and C is : (E is mid-point of arm CD)



   (a) R (b) $\frac{1}{16}R$ (c) $\frac{7}{64}R$ (d) $\frac{3}{4}R$

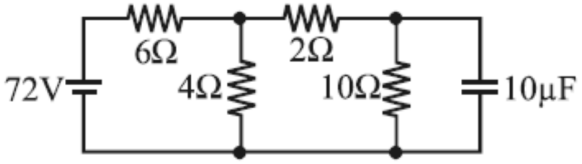
5. The total number of turns and cross-section area in a solenoid is fixed. However, its length L is varied by adjusting the separation between windings. The inductance of solenoid will be proportional to :

   (a) $1/L^2$ (b) $1/L$ (c) L (d) L^2

6. A simple pendulum oscillating in air has period T. The bob of the pendulum is completely immersed in a non-viscous liquid. The density of the liquid is $\frac{1}{16}$th of the material of the bob. If the bob is inside liquid all the time, its period of oscillation in this liquid is :

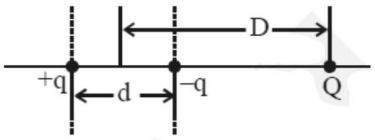
   (a) $4T\sqrt{\frac{1}{15}}$ (b) $2T\sqrt{\frac{1}{10}}$ (c) $4T\sqrt{\frac{1}{14}}$ (d) $2T\sqrt{\frac{1}{14}}$

7. Determine the charge on the capacitor in the following circuit;



   (a) 2 μC (b) 60 μC (c) 200 μC (d) 10 μC

8. A system of three charges are placed as shown in the figure :
If D >> d, the potential energy of the system is best given by :



(a) $\frac{1}{4\pi\varepsilon_0}\left[-\frac{q^2}{d}-\frac{qQd}{2D^2}\right]$ (b) $\frac{1}{4\pi\varepsilon_0}\left[+\frac{q^2}{d}+\frac{qQd}{D^2}\right]$

(c) $\frac{1}{4\pi\varepsilon_0}\left[-\frac{q^2}{d}+\frac{2qQd}{D^2}\right]$ (d) $\frac{1}{4\pi\varepsilon_0}\left[-\frac{q^2}{d}-\frac{qQd}{D^2}\right]$

9. The stream of a river is flowing with a speed of 2km/h. A swimmer can swim at a speed of 4km/h. What should be the direction of the swimmer with respect to the flow of the river to cross the river straight?
(a) 60° (b) 150° (c) 90° (d) 120°

10. A body of mass 2 kg makes an eleastic collision with a second body at rest and continues to move in the original direction but with one fourth of its original speed. What is the mass of the second body ?
(a) 1.8 kg (b) 1.2 kg (c) 1.5 kg (d) 1.0 kg

11. A solid sphere of mass 'M' and radius 'a' is surrounded by a uniform concentric spherical shell of thickness 2a and mass 2M. The gravitational field at distance '3a' from the centre will be :
(a) $\frac{2GM}{9a^2}$ (b) $\frac{GM}{3a^2}$ (c) $\frac{GM}{9a^2}$ (d) $\frac{2GM}{3a^2}$

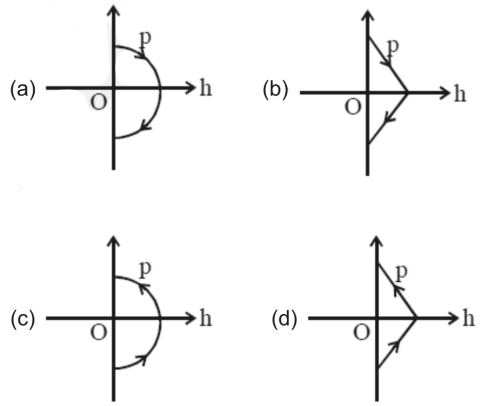
12. The pressure wave, P = 0.01 sin [1000t – 3x] Nm^{-2}, corresponds to the sound produced by a vibrating blade on a day when atmospheric temperature is 0°C. On some other day, when temperature is T, the speed of sound produced by the same blade and at the same frequency is found to be 336 ms^{-1}. Approximate value of T is :
(a) 15°C (b) 12°C (c) 4°C (d) 11°C

13. An NPN transistor is used in common emitter configuration as an amplifier with 1 $k\Omega$ load resistance. Signal voltage of 10 mV is applied across the base-emitter. This produces a 3 mA change in the collector current and 15 μA change in the base current of the amplifier. The input resistance and voltage gain are :
(a) 0.33 $k\Omega$, 1.5 (b) 0.67 $k\Omega$, 200 (c) 0.33 $k\Omega$, 300 (d) 0.67 $k\Omega$, 300

14. A moving coil galvanometer has resistance 50 Ω and it indicates full deflection at 4mA current. A voltmeter is made using this galvanometer and a 5 $k\Omega$ resistance. The maximum voltage, that can be measured using this voltmeter, will be close to :
(a) 10 V (b) 20 V (c) 40 V (d) 15 V

15. The electric field of light wave is given as $\vec{E}=10^{-3}\cos\left(\frac{2\pi x}{5\times10^{-7}}-2\pi\times6\times10^{14}t\right)\hat{x}\frac{N}{C}$. This light falls on a metal plate of work function 2eV. The stopping potential of the photo-electrons is : Given E (in eV) $=\frac{12375}{\lambda(\text{in}\,\text{Å})}$.
(a) 0.48 V (b) 2.0 V (c) 2.48 V (d) 0.72 V

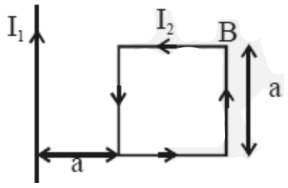
16. A ball is thrown vertically up (taken as +z-axis) from the ground. The correct momentum-height (p-h) diagram is :



17. A capacitor with capacitance 5 μF is charged to 5 μC. If the plates are pulled apart to reduce the capacitance to 2 μF, how much work is done?

(a) 3.75×10^{-6} J (b) 2.55×10^{-6} J (c) 2.16×10^{-6} J (d) 6.25×10^{-6} J

18. A rigid square loop of side 'a' and carrying current I_2 is lying on a horizontal surface near a long current I_1 carrying wire in the same plane as shown in figure. The net force on the loop due to wire will be :



(a) Attractive and equal to $\frac{\mu_0 I_1 I_2}{3\pi}$ (b) Repulsive and equal to $\frac{\mu_0 I_1 I_2}{4\pi}$

(c) Repulsive and equal to $\frac{\mu_0 I_1 I_2}{2\pi}$ (c) Zero

19. The figure shows a Young's double slit experimental setup. It is observed that when a thin transparent sheet of thickness t and refractive index μ is put in front of one of the slits, the central maximum gest shifted by a distance equal to n fringe widths. If the wavelength of light used is λ, t will be :

(a) $\frac{2D\lambda}{a(\mu-1)}$ (b) $\frac{D\lambda}{a(\mu-1)}$ (c) $\frac{2nD\lambda}{a(\mu-1)}$ (d) $\frac{nD\lambda}{a(\mu-1)}$

20. A string is clamped at both the ends and it is vibrating in its 4^{th} harmonic. The equation of the stationary wave is $Y = 0.3 \sin(0.157x) \cos(200\pi t)$. The length of the string is : (All quantities are in SI units.)

(a) 20 m (b) 80 m (c) 60 m (d) 40 m

21. The following bodies are made to roll up (without slipping) the same inclined plane from a horizontal plane. : (i) a ring of radius R, (ii) a solid cylinder of radius $\frac{R}{2}$ and (iii) a solid sphere of radius $\frac{R}{4}$. If in each case, the speed of the centre of mass at the bottom of the incline is same, the ratio of the maximum heights they climb is :

(a) 4 : 3 : 2 (b) 14 : 15 : 20 (c) 10 : 15 : 7 (d) 2 : 3 : 4

22. A stationary horizontal disc is free to rotate about its axis. When a torque is applied on it, its kinetic energy as a function of θ, where θ is the angle by which it has rotated, is given as $k\theta^2$. If its moment of inertia is I then the angular acceleration of the disc is :

(a) $\frac{k}{2I}\theta$ (b) $\frac{k}{I}\theta$ (c) $\frac{k}{4I}\theta$ (d) $\frac{2k}{I}\theta$

23. A uniform cable of mass 'M' and length 'L' is placed on a horizontal surface such that its $\left(\frac{1}{n}\right)^{th}$ part is hanging below the edge of the surface. To lift the hanging part of the cable upto the surface, the work done should be :

(a) $\frac{MgL}{n^2}$ (b) $\frac{MgL}{2n^2}$ (c) $\frac{2MgL}{n^2}$ (d) nMgL

24. If 'M' is the mass of water that rises in a capillary tube of radius 'r', then mass of water which will rise in a capillary tube of radius '2r' is :

(a) 4M (b) M (c) 2M (d) $\frac{M}{2}$

25. Taking the wavelength of first Balmer line in hydrogen spectrum (n = 3 to n = 2) as 660 nm, the wavelength of the 2^{nd} Balmer line (n = 4 to n = 2) will be :

(a) 889.2 nm (b) 642.7 nm (c) 488.9 nm (d) 388.9 nm

26. The magnetic field of a plane electromagnetic wave is given by :

$\vec{B} = B_0\hat{i}[\cos(kz - \omega t] + B_1\hat{j}\cos(kz + \omega t)$ where $B_0 = 3\times10^{-5}$ T and $B_1 = 2\times10^{-6}$ T. The rms value of the force experienced by a stationary charge $Q = 10^{-4}$ C at $z = 0$ is closest to :

(a) 0.9 N (b) 0.1 N (c) 3×10^{-2} N (d) 0.6 N

27. A rectangular coil (Dimension 5 cm × 2.5 cm) with 100 turns, carrying a current of 3 A in the clock-wise direction is kept centered at the origin and in the X-Z plane. A magnetic field of 1 T is applied along X-axis. If the coil is tilted through 45° about Z-axis, then the torque on the coil is :

(a) 0.55 Nm (b) 0.27 Nm (c) 0.38 (d) 0.42 Nm

28. A concave mirror for face viewing has focal length of 0.4 m. The distance at which you hold the mirror from your face in order to see your image upright with a magnification of 5 is :

(a) 1.60 m (b) 0.24 m (c) 0.16 m (d) 0.32 m

29. A signal $A\cos\omega t$ is transmitted using $\nu_0 \sin\omega_0 t$ as carrier wave. The correct amplitude modulated (AM) signal is :

(a) $\nu_0\sin\omega_0 t + A\cos\omega t$ (b) $\nu_0\sin\omega_0 t + \frac{A}{2}\sin(\omega_0 - \omega)t + \frac{A}{2}\sin(\omega_0 + \omega)t$

(c) $(\nu_0 + A)\cos\omega t\sin\omega_0 t$ (d) $\nu_0\sin[\omega_0(1 + 0.01A\sin\omega t)t]$

30. For a given gas at 1 atm pressure, rms speed of the molecule is 200 m/s at 127°C. At 2 atm pressure and at 227°C, the rms speed of the molecules will be :

(a) 80 m/s (b) $100\sqrt{5}$ m/s (c) $80\sqrt{5}$ m/s (d) 100 m/s

Chemistry

31. The correct order of the oxidation states of nitrogen in NO, N_2O, NO_2 and N_2O_3 is :

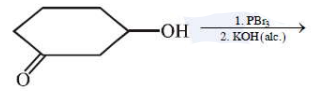
(a) $NO_2 < N_2O_3 < NO < N_2O$ (b) $NO_2 < NO < N_2O_3 < N_2O$

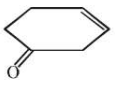
(c) $N_2O < N_2O_3 < NO < NO_2$ (d) $N_2O < NO < N_2O_3 < NO_2$

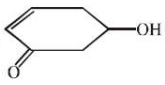
32. The degenerate orbitals of $[Cr(H_2O)_6]^{3+}$ are :

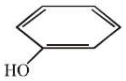
(a) d_{yz} and d_{z^2} (b) d_{z^2} and d_{xz} (c) d_{xz} and d_{yz} (d) $d_{x^2-y^2}$ and d_{xy}

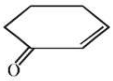
33. The major product of the following reaction is :



(a) 

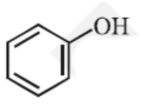
(b) 

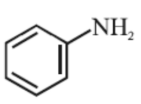
(c) 

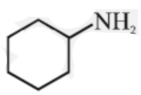
(d) 

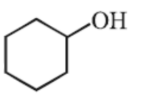
34. The organic compound that gives following qualitative analysis is :

Test	Inference
(a) Dil. HCl	Insoluble
(b) NaOH solution	soluble
(c) Br_2/water	Decolourization

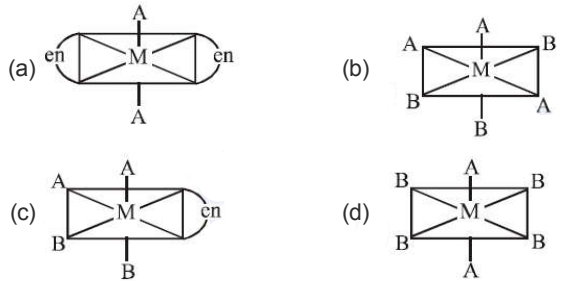
(a) 

(b) 

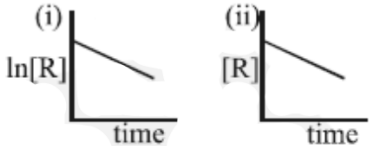
(c) 

(d) 

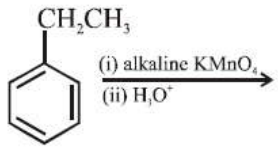
35. Which of the following statements is not true about sucrose?
    (a) On hydrolysis, it produces glucose and fructose
    (b) The glycosidic linkage is present between C_1 of α-glucose and C_1 of β-fructose
    (c) It is also named as invert sugar
    (d) It is a non reducing sugar
36. Excessive release of CO_2 into the atomosphere results in :
    (a) polar vortex (b) depletion of ozone
    (c) formation of smog (d) global warming
37. Among the following, the molecule expected to be stabilized by anion formation is : C_2, O_2, NO, F_2
    (a) NO (b) C_2 (c) F_2 (d) O_2
38. The one that will show optical activity is : (en = ethane-1, 2-diamine)

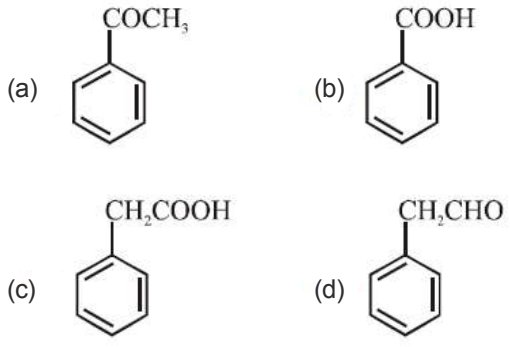


39. The given plots represent the variation of the concentration of a reactant R with time for two different reactions (i) and (ii). The respective orders of the reactions are :



    (a) 1, 0 (b) 1,1 (c) 0,1 (d) 0,2
40. The aerosol is a kind of colloid in which :
    (a) gas is dispersed in solid (b) solid is dispersed in gas
    (c) liquid is dispersed in water (d) gas is dispersed in liquid
41. The major product of the following reaction is :

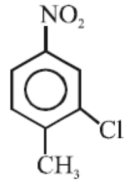




42. For a reaction, $N_2(g) + 3H_2(g) \rightarrow 2NH_3(g)$; identify dihydrogen (H_2) as a limiting reagent in the following reaction mixtures.
(a) 14g of N_2 + 4g of H_2 (b) 28g of N_2 + 6g of H_2
(c) 56g of N_2 + 10g of H_2 (d) 35g of N_2 + 8g of H_2

43. The number of water molecule(s) not coordinated to copper ion directly in $CuSO_4.5H_2O$, is :
(a) 4 (b) 3 (c) 1 (d) 2

44. The correct IUPAC name of the following compound is :



(a) 5-chloro-4-methyl-1-nitrobenzene (b) 2-methyl-5-nitro-1-chlorobenzene
(c) 3-chloro-4-methyl-1-nitrobenzene (d) 2-chloro-1-methyl-4-nitrobenzene

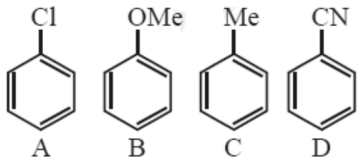
45. C_{60}, an allotrope of carbon contains :
(a) 20 hexagons and 12 pentagons. (b) 12 hexagons and 20 pentagons.
(c) 18 hexagons and 14 pentagons. (d) 16 hexagons and 16 pentagons.

46. Among the following, the set of parameters that represents path function, is :
(A) q + w (B) q (C) w (D) H–TS
(a) (A) and (D) (b) (B), (C) and (D) (c) (B) and (C) (d) (A), (B) and (C)

47. The osmotic pressure of a dilute solution of an ionic compound XY in water is four times that of a solution of 0.01 M $BaCl_2$ in water. Assuming complete dissociation of the given ionic compounds in water, the concentration of XY (in mol L^{-1}) in solution is :
(a) 6×10^{-2} (b) 4×10^{-4} (c) 16×10^{-4} (d) 4×10^{-2}

48. The standard Gibbs energy for the given cell reaction in kJ mol^{-1} at 298 K is :
$Zn(s) + Cu^{2+}(aq) \rightarrow Zn^{2+}(aq) + Cu(s)$, $E° = 2$ V at 298 K
(Faraday's constant, F = 96000 C mol^{-1})
(a) −384 (b) −192 (c) 192 (d) 384

49. The increasing order of reactivity of the following compounds towards aromatic electrophilic substitution reaction is :



(a) D < B < A < C (b) A < B < C < D (c) D < A < C < B (d) B < C < A < D

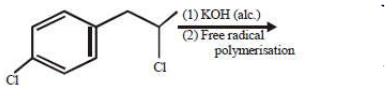
50. The ore that contains the metal in the form of fluoride is :
(a) magnetite (b) sphalerite (c) malachite (d) cryolite

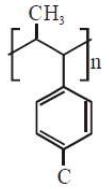
51. Consider the van der Waals constants, a and b, for the following gases.

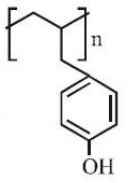
Gas	Ar	Ne	Kr	Xe
a/ (atm dm^6 mol^{-2})	1.3	0.2	5.1	4.1
b/ (10^{-2} dm^3 mol^{-1}	3.2	1.7	1.0	5.0

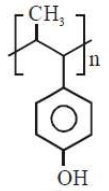
Which gas is expected to have the highest critical temperature?
(a) Kr (b) Ne (c) Ar (d) Xe

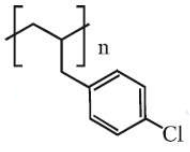
52. The major product of the following reaction is :



(a) 

(b) 

(c) 

(d) 

53. The major product of the following reaction is :

$CH_3CH = CHCO_2CH_3 \xrightarrow{LiAlH_4}$

(a) $CH_3CH_2CH_2CHO$
(b) $CH_3CH = CHCH_2OH$
(c) $CH_3CH_2CH_2CO_2CH_3$
(d) $CH_3CH_2CH_2CH_2OH$

54. Magnisium powder burns in air to give:

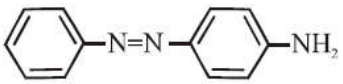
(a) MgO only
(b) MgO and $Mg(NO_3)_2$
(c) MgO and Mg_3N_2
(d) $Mg(NO_3)_2$ and Mg_3N_2

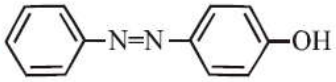
55. Liquid 'M' and liquid 'N' form an ideal solution. The vapour pressures of pure liquids 'M' and 'N' are 450 and 700 mmHg, respectively, at the same temperature. Then correct statement is:

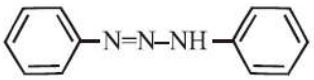
(x_M = Mole fraction of 'M' in solution ;
x_N = Mole fraction of 'N' in solution ;
y_M = Mole fraction of 'M' in vapour phase ;
y_N = Mole fraction of 'N' in vapour phase)

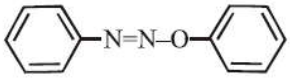
(a) $(x_M - y_M) < (x_N - y_N)$
(b) $\frac{x_M}{x_N} < \frac{y_M}{y_N}$
(c) $\frac{x_M}{x_N} > \frac{y_M}{y_N}$
(d) $\frac{x_M}{x_N} = \frac{y_M}{y_N}$

56. Aniline dissolved in dilute HCl is reacted with sodium nitrite at 0°C. This solution was added dropwise to a solution containing equimolar mixture of aniline and phenol in dil. HCl. The structure of the major product is :

(a) 

(b) 

(c) 

(d) 

57. The element having greatest difference between its first and second ionization energies, is :
(a) Ca (b) K (c) Ba (d) Sc

58. For any given series of spectral lines of atomic hydrogen, let $\Delta\bar{\nu} = \bar{\nu}_{max} - \bar{\nu}_{min}$ be the difference in maximum and minimum frequencies in cm^{-1}. The ratio $\Delta\bar{\nu}_{Lyman} = \Delta\bar{\nu}_{Balmer}$ is :
(a) 27 : 5 (b) 4 : 1 (c) 5 : 4 (d) 9 : 4

59. The major product of the following reaction is :
$CH_3C\equiv CH \xrightarrow[(ii)\ DI]{(i)\ DCl\ (1equiv.)}$
(a) $CH_3CD(Cl)CHD(I)$ (b) $CH_3CD_2CH(Cl)(I)$
(c) $CH_3CD(I)CHD(Cl)$ (d) $CH_3C(I)(Cl)CHD_2$

60. Match the catalysts **(Column I)** with products **(Column II)**.

Column I	**Column II**
(a) V_2O_5	(i) Polyethylene
(b) $TiCl_4/Al(Me)_3$	(ii) ethanal
(c) $PdCl_2$	(iii) H_2SO_4
(d) Iron Oxide	(iv) NH_3

(a) (A)-(ii); (B)-(iii); (C)-(i); (D)-(iv) (b) (A)-(iii); (B)-(i); (C)-(ii); (D)-(iv)
(c) (A)-(iii); (B)-(iv); (C)-(i); (D)-(ii) (d) (A)-(iv); (B)-(iii); (C)-(ii); (D)-(i)

Mathematics

61. Let $\vec{\alpha} = 3\hat{i} + \hat{j}$ and $\vec{\beta} = 2\hat{i} - \hat{j} + 3\hat{k}$. If $\vec{\beta} = \vec{\beta}_1 - \vec{\beta}_2$, where $\vec{\beta}_1$ is parallel to $\vec{\alpha}$ and $\vec{\beta}_2$ is perpendicular to $\vec{\alpha}$, then $\vec{\beta}_1 \times \vec{\beta}_2$ is equal to
(a) $-3\hat{i} - 9\hat{j} + 5\hat{k}$ (b) $3\hat{i} - 9\hat{j} - 5\hat{k}$ (c) $\frac{1}{2}(-3\hat{i} + 9\hat{j} + 5\hat{k})$ (d) $\frac{1}{2}(3\hat{i} - 9\hat{j} + 5\hat{k})$

62. For any two statements p and q, the negation of the expression $p \vee (\sim p \wedge q)$ is
(a) $p \wedge q$ (b) $p \leftrightarrow q$ (c) $\sim p \vee \sim q$ (d) $\sim p \wedge \sim q$

63. The value of $\int_0^{\pi/2} \frac{\sin^3 x}{\sin x + \cos x}\,dx$ is
(a) $\frac{\pi - 2}{4}$ (b) $\frac{\pi - 2}{8}$ (c) $\frac{\pi - 1}{4}$ (d) $\frac{\pi - 1}{2}$

64. If $f(x)$ is a non-zero polynomial of degree four, having local extreme points at $x = -1, 0, 1$; then the set $S = \{x \in R : f(x) = f(0)\}$ Contains exactly :
(a) four irrational numbers. (b) two irrational and one rational number.
(c) four rational numbers. (d) two irrational and two rational numbers.

65. If the standard deviation of the numbers $-1, 0, 1, k$ is $\sqrt{5}$ where $k > 0$, then k is equal to
(a) $2\sqrt{\frac{10}{3}}$ (b) $2\sqrt{6}$ (c) $4\sqrt{\frac{5}{3}}$ (d) $\sqrt{6}$

66. All the points in the set $S = \left\{\frac{\alpha + i}{\alpha - i} : a \in R\right\}$ $(i = \sqrt{-1})$ lie on a
(a) circle whose radius is 1. (b) straight line whose slope is 1.
(c) straight line whose slope is -1 (d) circle whose radius is $\sqrt{2}$

67. Let S be the set of all values of x for which the tangent to the curve $y = f(x) = x^3 - x^2 - 2x$ at (x, y) is parallel to the line segment joining the points $(1, f(1))$ and $(-1, f(-1))$, then S is equal to :

(a) $\left\{-\frac{1}{3}, -1\right\}$ (b) $\left\{\frac{1}{3}, -1\right\}$ (c) $\left\{-\frac{1}{3}, 1\right\}$ (d) $\left\{\frac{1}{3}, 1\right\}$

68. Let $f(x) = 15 - |x - 10|$; $x \in R$. Then the set of all values of x, at which the function, $g(x) = f(f(x))$ is not differentiable, is :

(a) {5, 10, 15, 20} (b) {10, 15} (c) {5, 10, 15} (d) {10}

69. Let $p, q \in R$. If $2 - \sqrt{3}$ is a root of the quadratic equation, $x^2 + px + q = 0$, then :

(a) $q^2 + 4p + 14 = 0$ (b) $p^2 - 4q - 12 = 0$

(c) $q^2 - 4p - 16 = 0$ (d) $p^2 - 4q + 12 = 0$

70. Slope of a line passing through P(2, 3) and intersecting the line, $x + y = 7$ at a distance of 4 units from P, is

(a) $\frac{\sqrt{5}-1}{\sqrt{5}+1}$ (b) $\frac{1-\sqrt{5}}{1+\sqrt{5}}$ (c) $\frac{1-\sqrt{7}}{1+\sqrt{7}}$ (d) $\frac{\sqrt{7}-1}{\sqrt{7}+1}$

71. A committee of 11 members is to be formed from 8 males and 5 females. If m is the number of ways the committee is formed with at least 6 males and n is the number of ways the committee is formed with at least 3 females, then :

(a) $m = n = 78$ (b) $n = m - 8$ (c) $m + n = 68$ (d) $m = n = 68$

72. If the fourth term in the binomial expansion of $\left(\frac{2}{x} + x^{\log_8 x}\right)^6$ $(x > 0)$ is 20×8^7, then a value of x is :

(a) 8 (b) 8^2 (c) 8^{-2} (d) 8^3

73. The solution of the differential equation $x\frac{dy}{dx} + 2y = x^2$ $(x \neq 0)$ with $y(1) = 1$, is

(a) $y = \frac{x^3}{5} + \frac{1}{5x^2}$ (b) $y = \frac{4}{5}x^3 + \frac{1}{5x^2}$ (c) $y = \frac{3}{4}x^2 + \frac{1}{4x^2}$ (d) $y = \frac{x^2}{4} + \frac{3}{4x^2}$

74. A plane passing through the points (0, –1, 0) and (0, 0, 1) and making an angle $\frac{\pi}{4}$ with the plane $y - z + 5 = 0$, also passes through the point

(a) $\left(-\sqrt{2}, 1, -4\right)$ (b) $\left(\sqrt{2}, 1, 4\right)$ (c) $\left(\sqrt{2}, -1, 4\right)$ (d) $\left(-\sqrt{2}, -1, -4\right)$

75. The integral $\int \sec^{2/3}x \operatorname{cosec}^{4/3}x\, dx$ is equal to (Hence C is a constant of integration)

(a) $3\tan^{-1/3}x + C$ (b) $-\frac{3}{4}\tan^{-4/3}x + C$ (c) $-3\cot^{-1/3}x + C$ (d) $-3\tan^{-1/3}x + C$

76. Let the sum of the first n terms of a non-constant A.P., $a_1, a_2, a_4, \ldots$ be $50n + \frac{n(n-7)}{2}A$, where A is a constant. If d is the common difference of this A.P., then the ordered pair (d, a_{50}) is equal to

(a) (A, 50 + 46A) (b) (A, 50 + 45A) (c) (50, 50 + 46A) (d) (50, 50 + 45A)

77. The area (in sq. units) of the region $A = \{(x, y) : x^2 \leq y \leq x + 2\}$ is

(a) $\frac{10}{3}$ (b) $\frac{9}{2}$ (c) $\frac{31}{6}$ (d) $\frac{13}{6}$

78. If the line, $\frac{x-1}{2}=\frac{y+1}{3}=\frac{z-2}{4}$ meets the plane, x + 2y + 3z = 15 at a point P, then the distance of P from the origin is

(a) $\frac{9}{2}$ (b) $2\sqrt{5}$ (c) $\frac{\sqrt{5}}{2}$ (d) $\frac{7}{2}$

79. Let $\sum_{k=1}^{10} f(a+k)=16(2^{10}-1)$, where the function f satisfies $f(x+y)=f(x)f(y)$ for all natural numbers x, y and $f(1)=2$. then the natural number 'a' is

(a) 4 (b) 3 (c) 16 (d) 2

80. Let α and β be the roots of the equation $x^2 + x + 1 = 0$. Then for $y \neq 0$ in R, $\begin{vmatrix} y+1 & \alpha & \beta \\ \alpha & y+\beta & 1 \\ \beta & 1 & y+\alpha \end{vmatrix}$ is equal to

(a) y^3 (b) $y^3 - 1$ (c) $y(y^2 - 1)$ (d) $y(y^2 - 3)$

81. If the tangent to the curve, $y = x^3 + ax - b$ at the point (1, −5) is perpendicular to the line, $-x + y + 4 = 0$, then which one of the following points lies on the curve ?

(a) (−2, 2) (b) (2, −2) (c) (2, −1) (d) (−2, 1)

82. Four persons can it a target correctly with probabilities $\frac{1}{2}, \frac{1}{3}, \frac{1}{4}$ and $\frac{1}{8}$ respectively. If all hit at the target independently, then the probability that the target would be hit, is

(a) $\frac{25}{192}$ (b) $\frac{1}{192}$ (c) $\frac{25}{32}$ (d) $\frac{7}{32}$

83. If the line $y = mx + 7\sqrt{3}$ is normal to the hyperbola $\frac{x^2}{24}-\frac{y^2}{18}=1$, then a value of m is

(a) $\frac{\sqrt{5}}{2}$ (b) $\frac{3}{\sqrt{5}}$ (c) $\frac{2}{\sqrt{5}}$ (d) $\frac{\sqrt{15}}{2}$

84. Let $S = \{\theta \in [-2\pi, 2\pi] : 2\cos^2\theta + 2\sin\theta = 0\}$. Then the sum of the elements of S is

(a) $\frac{13\pi}{6}$ (b) π (c) 2π (d) $\frac{5\pi}{3}$

85. The value of $\cos^2 10° - \cos 10°\cos 50° + \cos^2 50°$ is

(a) $\frac{3}{2}(1+\cos 20°)$ (b) $\frac{3}{4}$ (c) $\frac{3}{4}+\cos 20°$ (d) $\frac{3}{2}$

86. If a tangent to the circle $x^2 + y^2 = 1$ intersects the coordinate axes at distinct points P and Q, then the locus of the mid-point of PQ is

(a) $x^2 + y^2 - 2xy = 0$ (b) $x^2 + y^2 - 16x^2y^2 = 0$
(c) $x^2 + y^2 - 4x^2y^2 = 0$ (d) $x^2 + y^2 - 2x^2y^2 = 0$

87. If the function f defined on $\left(\frac{\pi}{6}, \frac{\pi}{3}\right)$ by $f(x)=\begin{cases}\frac{\sqrt{2}\cos x-1}{\cot x-1}, & x\neq\frac{\pi}{4}\\ k, & x=\frac{\pi}{4}\end{cases}$ is continuous, then k is equal to

(a) $\frac{1}{2}$ (b) 1 (c) $\frac{1}{\sqrt{2}}$ (d) 2

88. If $\begin{bmatrix}1 & 1\\0 & 1\end{bmatrix}\begin{bmatrix}1 & 2\\0 & 1\end{bmatrix}\cdot\begin{bmatrix}1 & 3\\0 & 1\end{bmatrix}\ldots\ldots\begin{bmatrix}1 & n-1\\0 & 1\end{bmatrix}=\begin{bmatrix}1 & 78\\0 & 1\end{bmatrix}$, then the inverse of $\begin{bmatrix}1 & n\\0 & 1\end{bmatrix}$ is

(a) $\begin{bmatrix}1 & -13\\0 & 1\end{bmatrix}$ (b) $\begin{bmatrix}1 & 0\\12 & 1\end{bmatrix}$ (c) $\begin{bmatrix}1 & -12\\0 & 1\end{bmatrix}$ (d) $\begin{bmatrix}1 & 0\\13 & 1\end{bmatrix}$

89. If one end of a focal chord of the parabola, $y^2 = 16x$ is at (1, 4), then the length of this focal chord is

(a) 25 (b) 24 (c) 20 (d) 22

90. If the function $f : R - \{1, -1\} \to A$ defined by $f(x)=\frac{x^2}{1-x^2}$, is subjective, then A is equal to

(a) $R - [-1, 0)$ (b) $R - (-1, 0)$ (c) $R - \{-1\}$ (d) $[0, \infty)$

PCM Answers

1	b	11	b	21	c	31	d	41	b	51	a	61	c	71	a	81	b
2	c	12	c	22	d	32	c	42	c	52	a	62	d	72	b	82	c
3	b	13	d	23	b	33	d	43	c	53	b	63	c	73	d	83	c
4	c	14	b	24	c	34	a	44	d	54	c	64	b	74	b	84	c
5	b	15	a	25	c	35	b	45	a	55	c	65	b	75	d	85	b
6	a	16	a	26	d	36	d	46	c	56	a	66	a	76	a	86	c
7	c	17	a	27	b	37	b	47	a	57	b	67	c	77	b	87	a
8	d	18	b	28	d	38	c	48	a	58	d	68	c	78	a	88	a
9	d	19	d	29	b	39	a	49	c	59	d	69	b	79	b	89	a
10	b	20	b	30	b	40	b	50	d	60	b	70	c	80	a	90	a